

BC Review 14 No Calculator

Do all work on separate notebook paper

_____ 1.

$$\int_0^1 \sqrt{x}(x+1) dx =$$

- (A) 0 (B) 1 (C) $\frac{16}{15}$ (D) $\frac{7}{5}$ (E) 2

_____ 2.

If $x = e^{2t}$ and $y = \sin(2t)$, then $\frac{dy}{dx} =$

- (A) $4e^{2t}\cos(2t)$ (B) $\frac{e^{2t}}{\cos(2t)}$ (C) $\frac{\sin(2t)}{2e^{2t}}$ (D) $\frac{\cos(2t)}{2e^{2t}}$ (E) $\frac{\cos(2t)}{e^{2t}}$

_____ 3.

The function f given by $f(x) = 3x^5 - 4x^3 - 3x$ has a relative maximum at $x =$

- (A) -1 (B) $-\frac{\sqrt{5}}{5}$ (C) 0 (D) $\frac{\sqrt{5}}{5}$ (E) 1

_____ 4.

$$\frac{d}{dx} \left(x e^{\ln x^2} \right) =$$

- (A) $1+2x$ (B) $x+x^2$ (C) $3x^2$ (D) x^3 (E) x^2+x^3

_____ 5.

If $f(x) = (x-1)^{\frac{3}{2}} + \frac{e^{x-2}}{2}$, then $f'(2) =$

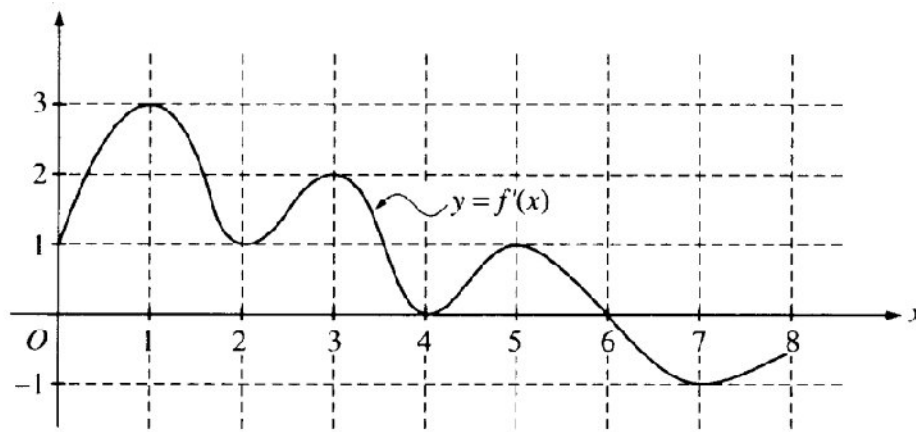
- (A) 1 (B) $\frac{3}{2}$ (C) 2 (D) $\frac{7}{2}$ (E) $\frac{3+e}{2}$

_____ 6.

The line normal to the curve $y = \sqrt{16-x}$ at the point $(0, 4)$ has slope

- (A) 8 (B) 4 (C) $\frac{1}{8}$ (D) $-\frac{1}{8}$ (E) -8

7.



The function f is defined on the closed interval $[0, 8]$. The graph of its derivative f' is shown above.

The point $(3, 5)$ is on the graph of $y = f(x)$. An equation of the line tangent to the graph of f at $(3, 5)$ is

- (A) $y = 2$
- (B) $y = 5$
- (C) $y - 5 = 2(x - 3)$
- (D) $y + 5 = 2(x - 3)$
- (E) $y + 5 = 2(x + 3)$

8. (Use graph above)

How many points of inflection does the graph of f have?

- (A) Two
- (B) Three
- (C) Four
- (D) Five
- (E) Six

9. (Use graph above)

At what value of x does the absolute minimum of f occur?

- (A) 0
- (B) 2
- (C) 4
- (D) 6
- (E) 8

_____ 10.

If $y = xy + x^2 + 1$, then when $x = -1$, $\frac{dy}{dx}$ is

- (A) $\frac{1}{2}$ (B) $-\frac{1}{2}$ (C) -1 (D) -2 (E) nonexistent

Free Response

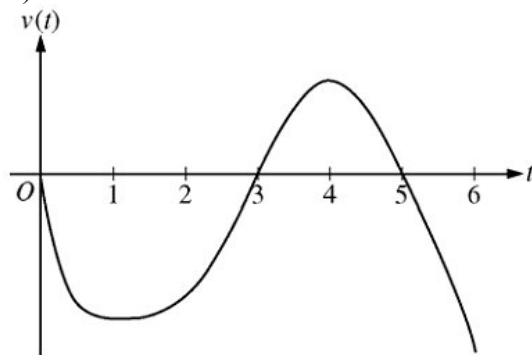
11. 2008—BC3 (Calculator Permitted)

x	$h(x)$	$h'(x)$	$h''(x)$	$h'''(x)$	$h^{(4)}(x)$
1	11	30	42	99	18
2	80	128	$\frac{488}{3}$	$\frac{448}{3}$	$\frac{584}{9}$
3	317	$\frac{753}{2}$	$\frac{1383}{4}$	$\frac{3483}{16}$	$\frac{1125}{16}$

Let h be a function having derivatives of all orders for $x > 0$. Selected values of h and its first four derivatives are indicated in the table above. The function h and these four derivatives are increasing on the interval $1 \leq x \leq 3$.

- (a) Write the first-degree Taylor polynomial for h about $x = 2$ and use it to approximate $h(1.9)$. Is this approximation greater than or less than $h(1.9)$? Explain your reasoning.
- (b) Write the third-degree Taylor polynomial for h about $x = 2$ and use it to approximate $h(1.9)$.
- (c) Use the Lagrange error bound to show that the third-degree Taylor polynomial for h about $x = 2$ approximates $h(1.9)$ with error less than 3×10^{-4} .

12. 2008—AB/BC4 (No Calculator)



Graph of v

A particle moves along the x -axis so that its velocity at time t , for $0 \leq t \leq 6$, is given by a differentiable function v whose graph is shown above. The velocity is 0 at $t = 0$, $t = 3$, and $t = 5$, and the graph has horizontal tangents at $t = 1$ and $t = 4$. The areas of the regions bounded by the t -axis and the graph of v on the intervals $[0, 3]$, $[3, 5]$, and $[5, 6]$ are 8, 3, and 2, respectively. At time $t = 0$, the particle is at $x = -2$.

- For $0 \leq t \leq 6$, find both the time and the position of the particle when the particle is farthest to the left. Justify your answer.
- For how many values of t , where $0 \leq t \leq 6$, is the particle at $x = -8$? Explain your reasoning.
- On the interval $2 < t < 3$, is the speed of the particle increasing or decreasing? Give a reason for your answer.
- During what time intervals, if any, is the acceleration of the particle negative? Justify your answer.