1.

A particle moves along a straight line with velocity given by $v(t) = 7 - (1.01)^{-t^2}$ at time $t \ge 0$. What is the acceleration of the particle at time t = 3?

- (A) 0.914
- (B) 0.055
- (C) 5.486
- (D) 6.086
- (E) 18.087

2.

х	-4	-3	-2	-1
f(x)	0.75	-1.5	-2.25	-1.5
f'(x)	-3	-1.5	0	1.5

The table above gives values of a function f and its derivative at selected values of x. If f' is continuous on the interval [-4, -1], what is the value of $\int_{-4}^{-1} f'(x) dx$?

- (A) -4.5
- (B) -2.25
- (C) 0
- (D) 2.25
- (E) 4.5

3.

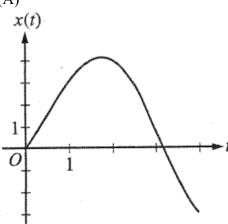
The radius of a sphere is decreasing at a rate of 2 centimeters per second. At the instant when the radius of the sphere is 3 centimeters, what is the rate of change, in square centimeters per second, of the surface area of the sphere? (The surface area S of a sphere with radius r is $S = 4\pi r^2$)

- (A) -108π
- (B) -72π
- (C) -48π
- (D) -24π
- (E) -16π

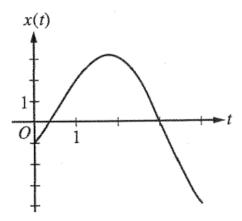
t	0	1	2	3	4
v(t)	-1	2	3	0	-4

The table gives selected values of the velocity, v(t), of a particle moving along the x-axis. At time t = 0, the particle is at the origin. Which of the following could be the graph of the position, x(t), of the particle for $0 \le t \le 4$?

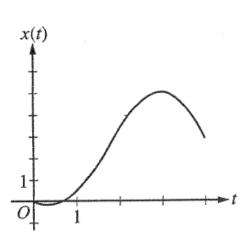
(A)



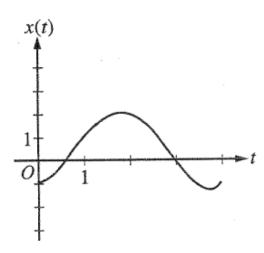
(B)



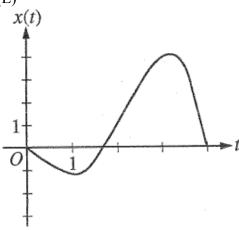
(C)



(D)



(E)



5.

The function f is continuous for $-2 \le x \le 2$ and f(-2) = f(2) = 0. If there is no c, where -2 < c < 2, for which f'(c) = 0, which of the following statements must be true?

(A) For
$$-2 < k < 2$$
, $f'(k) > 0$.

(B) For
$$-2 < k < 2$$
, $f'(k) < 0$.

(C) For
$$-2 < k < 2$$
, $f'(k)$ exists.

- (D) For -2 < k < 2, f'(k) exists, but f' is not continuous.
- (E) For some k, where -2 < k < 2, f'(k) does not exist.

6.

The function f is continuous on the closed interval [2, 4] and twice differentiable on the open interval (2, 4). If f'(3) = 2 and f''(x) < 0 on the open interval (2,4), which of the following could be a table of values for f?

(A)

х	f(x)
2	2.5
3	5
4	6.5

(B)

X	f(x)
2	2.5
3	5
4	7

(C)

х	f(x)
2	3
3	5
4	6.5

(D)

x	f(x)
2	3
3	5
4	7

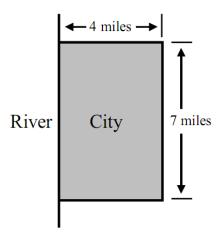
(E)

X	f(x)
2	3.5
3	5
4	7.5

What is the average value of $y = \frac{\cos x}{x^2 + x + 2}$ on the closed interval [-1, 3]?

- (A) -0.085
- (B) 0.090 (C) 0.183
- (D) 0.244
- (E) 0.732

8.



A city located beside a river has a rectangular boundary as shown in the figure above. The population density of the city at any point along a strip x miles from the river's edge is f(x) persons per square mile. Which of the following expressions gives the population of the city?

(A)
$$\int_0^4 f(x) dx$$

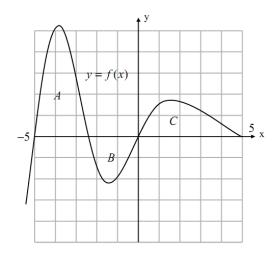
(B)
$$7 \int_{0}^{4} f(x) dx$$

(C)
$$28 \int_{0}^{4} f(x) dx$$

(D)
$$\int_0^7 f(x) dx$$

(E)
$$4\int_{0}^{7} f(x) dx$$

9.



The regions A, B, and C in the figure above are bounded by the graph of the function f and the x-axis.

If the area of each region is 2, what is the value of $\int_{5}^{-5} (f(x)-5)dx$?

- (A) 24
- (B) 36
- (C) 48
- (D) 60
- (E)72

10.

The rate of change of the altitude of a hot-air balloon is given by $r(t) = t^3 - 4t^2 + 6$ for $0 \le t \le 8$. Which of the following expressions gives the change in altitude of the balloon during the time the altitude is decreasing?

A)
$$\int_{1.572}^{3.514} r(t)dt$$

B)
$$\int_{0}^{8} r(t)dt$$

C)
$$\int_{0}^{2.667} r(t) dt$$

D)
$$\int_{1.572}^{3.514} r'(t)dt$$

E)
$$\int_{0}^{2.667} r'(t) dt$$

11. (2013, AB-1)

On a certain workday, the rate, in tons per hour, at which unprocessed gravel arrives at a gravel processing plant is modeled by $G(t) = 90 + 45\cos\left(\frac{t^2}{18}\right)$, where t is measured in hours and $0 \le t \le 8$. At the beginning of the workday (t = 0), the plant has 500 tons of unprocessed gravel. During the hours of operation, $0 \le t \le 8$, the plant processes gravel at a constant rate of 100 tons per hour.

- (a) Find G'(5). Using correct units, interpret your answer in the context of the problem.
- (b) Find the total amount of unprocessed gravel that arrives at the plant during the hours of operation on this workday.
- (c) Is the amount of unprocessed gravel at the plant increasing or decreasing at time t = 5 hours? Show the work that leads to your answer.
- (d) What is the maximum amount of unprocessed gravel at the plant during the hours of operation on this workday? Justify your answer.

12. (2013, AB-2) (Calculator Permitted)

A particle moves along a straight line. For $0 \le t \le 5$, the velocity of the particle is given by $v(t) = -2 + (t^2 + 3t)^{6/5} - t^3$, and the position of the particle is given by s(t). It is known that s(0) = 10.

- (a) Find all values of t in the interval $2 \le t \le 4$ for which the speed of the particle is 2.
- (b) Write an expression involving an integral that gives the position s(t). Use this expression to find the position of the particle at time t = 5.
- (c) Find all times t in the interval $0 \le t \le 5$ at which the particle changes direction. Justify your answer.
- (d) Is the speed of the particle increasing or decreasing at time t = 4? Give a reason for your answer.