

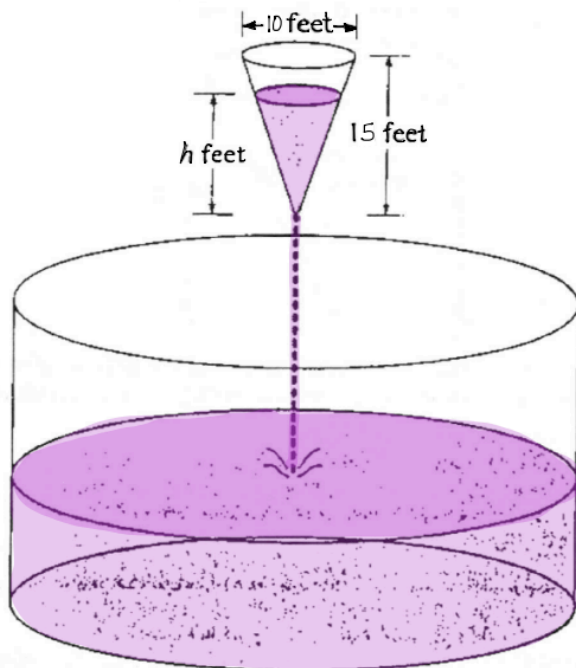
AP Calculus TEST: 3.1 to 4.1, **No Calculator**

I. Multiple Choice: Put the correct CAPITAL letter in the blank to the left of the question number.

- \_\_\_\_\_ 1. Let  $f$  be a differentiable function such that  $f(3) = 2$  and  $f'(3) = 5$ . If the tangent line at  $x = 3$  is used to find an approximation to a zero of  $f$ . That approximation is which of the following?
- (A) 0.4  
(B) 0.5  
(C) 2.6  
(D) 3.4  
(E) 5.5
- \_\_\_\_\_ 2. The radius of a spherical ball is decreasing at a constant rate of 3 cm per second. Find, in cubic centimeters per second, the rate of change of the volume of the ball when the radius is 5 cm.
- (A)  $-60\pi$   
(B)  $-150\pi$   
(C)  $-300\pi$   
(D)  $-12\pi$   
(E)  $-100\pi$
- \_\_\_\_\_ 3. If  $f'(x) = \sqrt[4]{x^3} - \frac{2}{\sqrt[3]{x^2}}$ , then what is  $f(x)$ , the general antiderivative of  $f'(x)$ ?
- (A)  $f(x) = \frac{7}{4}x \cdot \sqrt[4]{x^3} - \frac{5}{6}x \cdot \sqrt[3]{x^2} + C$   
(B)  $f(x) = \frac{4}{7}x \cdot \sqrt[4]{x^3} - 6 \cdot \sqrt[3]{x} + C$   
(C)  $f(x) = \frac{4}{7}x \cdot \sqrt[4]{x^3} - \frac{6}{5}x \cdot \sqrt[3]{x^2} + C$   
(D)  $f(x) = \frac{4}{7}\sqrt[4]{x^3} - \frac{2}{3}\sqrt[3]{x} + C$   
(E)  $f(x) = \frac{3}{4\sqrt[4]{x}} - \frac{4}{3\sqrt[3]{x}} + C$
- \_\_\_\_\_ 4. A street light is hung 18 feet above street level. A 6-foot tall man standing directly under the light walks away at a rate of 3 ft/sec. How fast is the tip of the man's shadow moving?
- (A)  $\frac{7}{2}$  ft/sec  
(B) 3 ft/sec  
(C)  $\frac{9}{2}$  ft/sec  
(D)  $\frac{1}{2}$  ft/sec  
(E)  $\frac{3}{2}$  ft/sec

- \_\_\_\_\_ 5. The graph of  $f(x) = 8x^5 - 5x^4$  will have how many points of inflection?
- (A) Four
  - (B) Two
  - (C) Three
  - (D) One
  - (E) None
- \_\_\_\_\_ 6. The sum of two positive integers is 90. If the product of one integer and the square of the other is a maximum, then the greater integer is
- (A) 60
  - (B) 50
  - (C) 75
  - (D) 55
  - (E) 80
- \_\_\_\_\_ 7. The shortest distance from the curve  $y = \sqrt{x}$  to the point  $(4, 0)$  is
- (A)  $\frac{\sqrt{15}}{2}$
  - (B)  $\frac{\sqrt{14}}{2}$
  - (C)  $\frac{7}{2}$
  - (D)  $\sqrt{15}$
  - (E)  $\sqrt{14}$
- \_\_\_\_\_ 8. Which of the given functions does NOT satisfy the conditions of the Mean Value Theorem on the interval  $x \in [-2, 2]$ ?
- I.  $f(x) = \frac{x^4}{4} - \frac{x^2}{2} - x$
  - II.  $f(x) = x^{2/3} - \frac{3}{x^2}$
  - III.  $f(x) = x^2 + \frac{1}{2x}$
- (A) I, II, and III    (B) I and III only    (C) II only    (D) II and III only    (E) III only
- \_\_\_\_\_ 9. The function defined by  $f(x) = 8x^2 - 2x^4$  has
- (A) No local extrema
  - (B) Two local maxima and one local minimum
  - (C) Two local maxima and two local minima
  - (D) Two local minima and one local maximum
  - (E) One local maximum and one local minimum

II. Free Response: Show all work in the space provided using correct notation. Include units on all final answers.



10. As shown in the figure above, Kool-Aid is draining from a conical tank with height 15 feet and diameter 10 feet into a cylindrical tank that has a base with area  $900\pi$  square feet. The depth,  $h$ , in feet, of the Kool-Aid in the conical tank is changing at the rate of  $\frac{dh}{dt} = h - 12$  feet per minute.

(a) Write an expression for the volume of Kool-Aid in the conical tank as a function of  $h$ .

(b) At what rate is the volume of Kool-Aid in the conical tank changing when  $h = 3$ ? Indicate units of measure. **Write a sentence, with units, explaining what your answer means in the context of the problem.**

(c) Let  $y$  be the depth, in feet, of the Kool-Aid in the cylindrical tank. At what rate is  $y$  changing when  $h = 3$ ? Indicate units of measure.