Lesson 7—Skills 26-30

Skill 26: Coordinates of a Circle

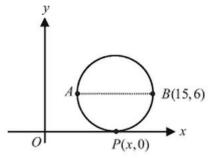
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When given questions regarding coordinates of a circle, tools such as the Pythagorean Theorem, Midpoint formula and/or Distance formulas can be used. Remember that the **diameter** is the width of the circle and runs through the center of the circle. The **radius** is half the diameter. Being **tangent** to a line means touching it once.

Pythagorean Theorem:
$$a^2 + b^2 = c^2$$

Midpoint formula: $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$
istance formula: $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Example 26:



In the figure above, *AB* is a diameter of the circle and parallel to the *x*-axis. What is the value of *x*?

Skill 27: Paths in a Grid

For these types of problems, you will be given a square or rectangular grid with two or more points labeled on the grid. You will be asked to determine how many different paths are possible between these points using vertical and/or horizontal sequences.

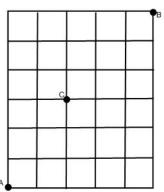
From earlier, we can use our combination formula for arrangements when order does NOT matter:

$$_{n}C_{r} = C(n,r) = \frac{n!}{r!(n-r)!}$$

Where n is the minimum number of moves required along any path and r is **either** the number of vertical **or** horizontal moves (it works out the same either way).

Also, remember to multiply independent events together to get a total.

Example 27:



In the figure above, a path from point A to point B is determined by moving upward or to the right along the grid lines.

- (a) How many different paths can be drawn from *A* to *B*?
- (b) How many different paths can be drawn from *A* to *B* that <u>must</u> include point *C*?

(c) How many different paths can be drawn from *A* to *B* that do <u>not</u> include point *C*?

Skill 28: Transformations

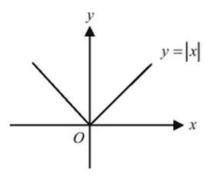
The types of transformations are

- Translations: involves "sliding" or "shifting" the object from one position to another. Shape and orientation are preserved.
- Reflections: involves "flipping" the object over a line called the line of reflections. Preserves shape, changes orientation.
- Rotation: involves "turning" the object about a pint called the center of rotation.
- Dilation: involves a "stretching" or "compressing" of an object. It changes the shape and/or size of the object, getting bigger or smaller (or narrower or wider).

If the graph of y = f(x) is translated *c* units horizontally and *d* units vertically, then the equation of the translated graph is

$$y-d = f(x-c)$$
 or $y = f(x-c)+d$

Example 28:



(a) If the graph of y = |x| is given above, what would the graph of y-3 = |x+5| look like? (b) If the graph of y = f(x) is given above, what would the graph of y = -|3-x|-5 look like?

Skill 29: The Least/Greatest Number

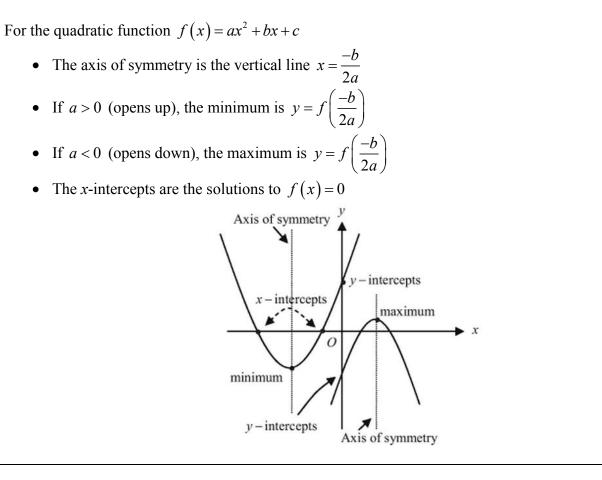
For these types of problems, you will be given an algebraic equation or inequality in two or more variables, then asked to predict an upper or lower bound for one of the variables. This requires a bit of algebra, thought, and practice.

Example 29:

- (a) If $0 \le x \le y$ and $(x+y)^2 (x-y)^2 \ge 64$, what is the least possible value of y?
- (b) If $x^2 y^2 \ge 77$ and x + y = 11, what is the greatest possible value of *y*?

Skill 30: Maximum & Minimum

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Example 30:

- (a) Given the equation $f(x) = x^2 2x 3$, find the equation of the axis of symmetry, the max/min value, and the *x*-intercept(s).
- (b) Given the equation $f(x) = -x^2 + 2x + 3$, find the equation of the axis of symmetry, the max/min value, and the *x*-intercept(s).