

AP Calc
 (2) Extreme Values
 Max: DNE
 Min: DNE
 No Rel Extrema.

(4) Extreme Values:
 Max: 2
 Min: -1
 Rel Max: 2
 Rel Min: -1

(6) Cont on closed interval, so guaranteed A
 Max & Min
 Max: $f(c)$
 Min: $f(b)$

(8) No guarantee by E.V.T.
 Rel Max is $f(b)$
 No Max or Min

(10) No guarantee by EVT. Rel Min $x=c$
 Max: $f(a)$
 Min: $f(c)$

(12) $g(x) = e^{-x}, -1 \leq x \leq 1$
 Max: $g(-1) = e$
 Min: $g(1) = e^{-1} = \frac{1}{e}$
 $g'(x) = -e^{-x} \neq 0$
 No CVS.

(14) $K(x) = e^{-x^2}, -\infty < x < \infty$
 Max: $g(0) = 1$
 No Min (H.A. @ $y=0$)
 $K'(x) = -2xe^{-x^2} = 0$
 $x=0$ c.v.
 $K(0) = 1$

(16) $g(x) = \sec x, -\frac{\pi}{2} < x < \frac{3\pi}{2}$
 $g'(x) = \sec x \tan x = 0$
 $\sec x = 0$
 $\cos x = \text{DNE}$
 No Sol.
 $\tan x = 0$
 $x = 0, \pi$
 $g(-\pi/2) = \infty$
 $g(3\pi/2) = -\infty$
 OPEN INTERVAL
 $g(0) = 1$
 $g(\pi) = -1$
 No Max or Min

(18) $f(x) = x^{3/5}, -2 < x \leq 3$
 $f'(x) = \frac{3}{5}x^{-2/5} = \frac{3}{5\sqrt[5]{x^2}} = \text{DNE}$
 when $x=0$
 $f(3) = \sqrt[5]{3^3} = \sqrt[5]{27}$ ← Max
 $f(0) = 0$ Not a min since open on left
 (∞ low approaching)
 $y = \sqrt[5]{-8}$

(26) $y = \frac{1}{\sqrt[3]{1-x^2}}$
 $x \neq \pm 1$
 $y = (1-x^2)^{-1/3}$
 $y' = -\frac{1}{3}(1-x^2)^{-4/3}(-2x)$
 $y' = \frac{2x}{3\sqrt[3]{(1-x^2)^4}}$
 $y' = 0$ @ $x=0$
 $y' = \text{DNE}$ @ $x = \pm 1$
 Not in domain of
 only c.v. @ $x=0$
 from graph: Local Min @ $(0, 1)$

(27) $y = \sqrt{3+2x-x^2}, D_y: -1 \leq x \leq 3$
 $y' = \frac{1}{2}(3+2x-x^2)^{-1/2}(-2x+2)$
 $= \frac{2-x}{\sqrt{3+2x-x^2}} = 0$
 when $x=2$
 $y' = \text{DNE}$ when $x = -1, 3$
 Rel Max @ $(2, \sqrt{3})$
 Max @ $(2, \sqrt{3})$
 Min @ $(-1, 0), (3, 0)$

(34) $K(x) = |x+1| + |x-3|, -\infty < x < \infty$
 $K'(x) = \text{DNE}$ @ $x = -1, 3$
 $K(-1) = 4$
 $K(3) = 4$
 $y = 4 \forall x \in (-1, 3)$
 Min value of $y = 4$

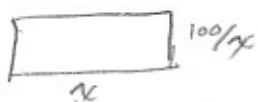
(37) $y = x\sqrt{4-x^2}$
 $y' = \sqrt{4-x^2} - \frac{2x^2}{2\sqrt{4-x^2}}$
 $= \frac{2(4-x^2) - 2x^2}{2\sqrt{4-x^2}}$
 $= \frac{8-4x^2}{2\sqrt{4-x^2}} = 0$
 when $x = \pm\sqrt{2}$
 $y' = \text{DNE}$ when $x = \pm 2$
 Rel Min @ $x = -\sqrt{2}, y = -2\sqrt{2}$
 Rel Max @ $x = \sqrt{2}, y = 2\sqrt{2}$

(40) $y = \begin{cases} 3-x, & x < 0 \\ 3+2x-x^2, & x \geq 0 \end{cases}$
 $y' = \begin{cases} -1, & x < 0 \\ 2-2x, & x \geq 0 \end{cases}$
 $x \rightarrow 0^- \implies y' = -1 + 2 = 1 = y'$
 $x \rightarrow 0^+ \implies y' = 2 - 2(0) = 2 = y'$
 So $x=0$ is a c.v.
 $y' = 0$ when $x=1$

Rel Min @ $x=0, y=3$
 Rel Max @ $x=1, y=4$

AP Calc AB C
§ 4.1 cont

(44) $P(x) = 2x + \frac{200}{x}$, $0 < x < \infty$

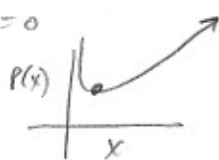


a) $P'(x) = 2 - \frac{200}{x^2} = 0$

$2 = \frac{200}{x^2}$

$x^2 = 100$

$x = 10$



$P'(x) = \text{DNE}$

$x = 0$

← Not in domain

Rel Min @ $x = 10$, $P(10) = 40$

b) The smallest Perimeter is 40 units, and it occurs when $x = 10$, which will make the Rectangle a 10×10 square.

(50) M.C. if $f(x)$ is Even (y-axis symm)

$\exists D_f \subset \mathbb{R}$ has local Max @ $x = a$, then

$f(-a) = f(a)$ since $f(x)$ is even.

↑ y-axis Reflection

So $f(-a)$ is ALSO a Local Max

B

(45) T or F:

If $f(c)$ is a Local Max of cont. function on (a,b) , then $f'(c) = 0$?

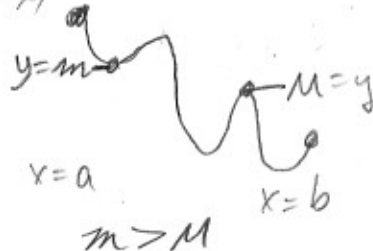
True, Rel Extrema occur at CVs, and if $f'(c) = 0$, then $v = 0$ is a c.v.

(46) T or F: If m is a

Local Min and M is a Local Max of cont function f on (a,b) , then $m < M$.

False:

ex)



(51) Let $f(x) = (x-2)^{2/3}$

a) Does $f'(2)$ exist?

$f'(x) = \frac{2}{3}(x-2)^{-1/3} = \frac{2}{3\sqrt[3]{x-2}}$

$f'(2) = \frac{2}{3\sqrt[3]{0}} = \text{DNE}$

So $f'(x)$ does not exist

b) Since $f(2)$ is defined ($= 0$), $x = 2 \in D_f$
So $x = 2$ is a c.v. of f



Since $f'(x) \neq 0$ and is only undefined at $x = 2$, $x = 2$ is the ONLY cv (Rel Extrema in this case.)

c) No, unless we specify a closed interval, we do not violate the EVT with only an abs min since the domain is OPEN (all \mathbb{R}_0)

d) For $f(x) = (x-a)^{2/3}$ everything above holds. We have only a Rel Min @ $x = a$.