AB: Practice Free Response. No Calculator. Show all work below line.

1. Let
$$f(x) = \begin{cases} x^2, & x \le 1 \\ 2x, & x > 1 \end{cases}$$

- a. Use the alternate form definition to find the left-hand derivative of f at x = 1 if it exists.
- b. Use the alternate form definition to find the right-hand derivative of f at x = 1 if it exists.
- c. Is f(x) differentiable at x = 1? Explain.
- d. Determine if f(x) is continuous at x = 1. Give conclusion based on the 3-step definition.
- e. Sketch a graph of f(x). Be sure to label it.
- f. On the same set of axes, sketch a graph of f'(x). Use a different line quality, and be sure to label it.

2. A particle moves along a horizontal line with position equation s(t) = (3t-2)(t-5) with s(t) measured

in feet t measured in seconds and $t \ge 0$.

- a. What is the initial position of the particle?
- b. When is the first time the particle is at zero?
- c. What is the particle's displacement on the interval from t = 0 to t = 2 seconds? Include units. Explain what that number means in terms of the particle's starting position.
- d. What is the particle's average velocity on the interval from t = 0 to t = 2 seconds? Include units.
- e. What is the particle's speed at t = 2 seconds? In which direction is it heading? Include units.
- f. What is the particle's acceleration at t = 2 seconds? Include units.
- g. At what time does the particle turn around?
- h. What is the particle's velocity when it is at zero for the second time?
- i. What is the particle's name?