

SEQUENCES AND SERIES
WORKSHEET 1

Do these problems on notebook paper. You may use your graphing calculator on problem 4 only,

1. Determine if the sequence $\left\{ \frac{\ln x}{x^2} \right\}$ converges.

2. Find the n th term (rule of sequence) of each sequence, and use it to determine whether or not the sequence converges.

(a) $2, \frac{3}{4}, \frac{4}{9}, \frac{5}{16}, \frac{6}{25}, \dots$

(b) $1, \frac{1}{2}, \frac{1}{6}, \frac{1}{24}, \frac{1}{120}, \dots$

3. Use the n th Term Divergence Test to determine whether or not the following *series* converge:

(a) $\sum_{n=1}^{\infty} \frac{1+3n^2+n^3}{4n^3-5n+2}$

(b) $\sum_{n=1}^{\infty} \frac{1}{n^2}$

(c) $\sum_{n=1}^{\infty} \frac{n!}{2n!+1}$

(d) $\sum_{n=1}^{\infty} \frac{(n+2)!}{10n!}$

4. (a) What is the sum of $\sum_{n=1}^{\infty} \left(\frac{1}{n+1} - \frac{1}{n+3} \right)$

(b) Using your calculator, calculate S_{500} to verify that the SOPS (sum of the partial sums) is bounded by the sum you found in part (a).

sum(seq(1/(N+1)-
1/(N+3), N, 1, 500))

5. Use the indicated test for convergence to determine if the series converges or diverges. If possible, state the value to which it converges.

(a) Geometric Series: $3 + \frac{15}{4} + \frac{75}{16} + \frac{375}{64} + \dots$

(b) Geometric Series: $\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \frac{1}{64} + \dots$

(c) p-series: $\sum_{n=1}^{\infty} n^{-2/3}$

(d) Integral Test: $\sum_{n=1}^{\infty} \frac{3n}{2n^2+3}$

(e) Direct Comparison: $\sum_{n=1}^{\infty} \frac{e^n}{n+3}$

(f) Direct Comparison: $\sum_{n=1}^{\infty} \frac{3^n}{7^n+1}$

(g) Limit Comparison: $\sum_{n=1}^{\infty} \frac{3n+6}{1-5n+7n^2}$

(h) Limit Comparison: $\sum_{n=1}^{\infty} \frac{n+5}{3n(4^n)}$

(i) Ratio Test: $\sum_{n=1}^{\infty} \frac{n^3}{n!}$

(j) Ratio Test: $\sum_{n=1}^{\infty} \frac{2}{n^2}$

(k) AST: $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n}$

(l) AST: $\sum_{n=1}^{\infty} \frac{(-1)^n(n+3)}{2n}$

(m) Direct Comparison: $\sum_{n=1}^{\infty} \frac{\sin n}{n^2}$

(n) Any method: $\sum_{n=1}^{\infty} \frac{(-1)^n(4^n)}{n!}$

6. Find the interval in which the actual sum of $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^2}$ is contained if S_5 is used to approximate it.