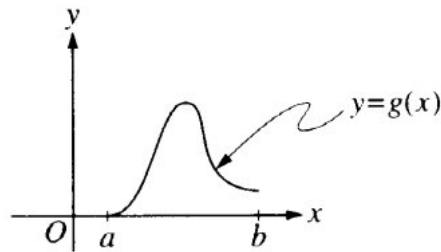
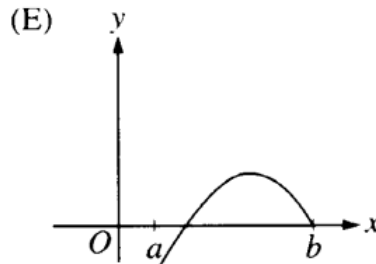
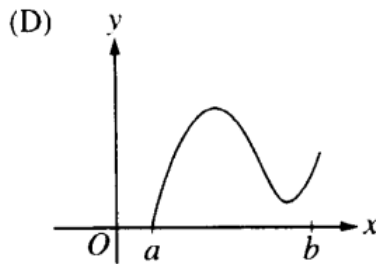
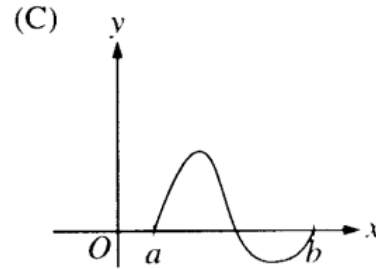
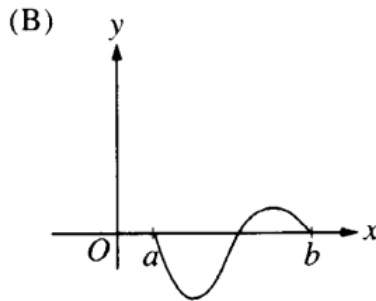
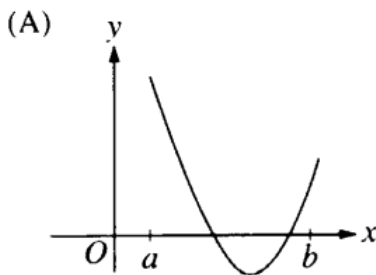


_____ 1.



Let $g(x) = \int_a^x f(t) dt$, where $a \leq x \leq b$. The figure above shows the graph of g on $[a, b]$. Which of the following could be the graph of f on $[a, b]$?



_____ 2.

The graph of the function represented by the Maclaurin series

$$1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots + \frac{(-1)^n x^n}{n!} + \dots$$

intersects the graph of $y = x^3$ at $x =$

- (A) 0.773 (B) 0.865 (C) 0.929 (D) 1.000 (E) 1.857

_____ 3.

Let f be the function given by $f(x) = x^2 - 2x + 3$. The tangent line to the graph of f at $x = 2$ is used to approximate values of $f(x)$. Which of the following is the greatest value of x for which the error resulting from this tangent line approximation is less than 0.5?

- (A) 2.4 (B) 2.5 (C) 2.6 (D) 2.7 (E) 2.8

4.

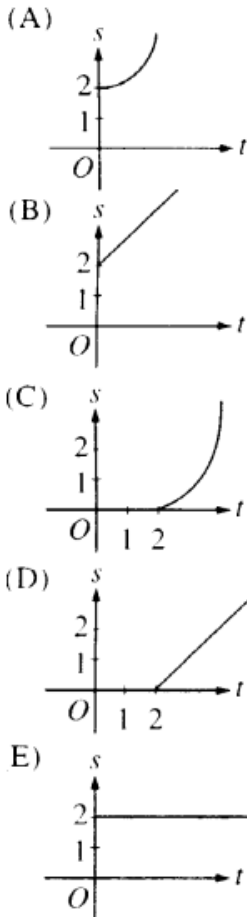
t (sec)	0	2	4	6
$a(t)$ (ft/sec ²)	5	2	8	3

The data for the acceleration $a(t)$ of a car from 0 to 6 seconds are given in the table above. If the velocity at $t = 0$ is 11 feet per second, the approximate value of the velocity at $t = 6$, computed using a left-hand Riemann sum with three subintervals of equal length, is

- (A) 26 ft/sec (B) 30 ft/sec (C) 37 ft/sec (D) 39 ft/sec (E) 41 ft/sec

5.

A particle starts from rest at the point $(2, 0)$ and moves along the x -axis with a constant positive acceleration for time $t \geq 0$. Which of the following could be the graph of the distance $s(t)$ of the particle from the origin as a function of time t ?



6.

If $0 \leq k < \frac{\pi}{2}$ and the area under the curve $y = \cos x$ from $x = k$ to $x = \frac{\pi}{2}$ is 0.1, then $k =$

- (A) 1.471 (B) 1.414 (C) 1.277 (D) 1.120 (E) 0.436

7.

Let f be a function that is differentiable on the open interval $(1,10)$. If $f(2) = -5$, $f(5) = 5$, and $f(9) = -5$, which of the following must be true?

- I. f has at least 2 zeros.
- II. The graph of f has at least one horizontal tangent.
- III. For some c , $2 < c < 5$, $f'(c) = 3$.

- (A) None
- (B) I only
- (C) I and II only
- (D) I and III only
- (E) I, II, and III

8.

If the base b of a triangle is increasing at a rate of 3 inches per minute while its height h is decreasing at a rate of 3 inches per minute, which of the following must be true about the area A of the triangle?

- (A) A is always increasing.
- (B) A is always decreasing.
- (C) A is decreasing only when $b < h$.
- (D) A is decreasing only when $b > h$.
- (E) A remains constant.

9.

If g is a differentiable function such that $g(x) < 0$ for all real numbers x and if $f'(x) = (x^2 - 4)g(x)$, which of the following is true?

- (A) f has a relative maximum at $x = -2$ and a relative minimum at $x = 2$.
- (B) f has a relative minimum at $x = -2$ and a relative maximum at $x = 2$.
- (C) f has relative minima at $x = -2$ and at $x = 2$.
- (D) f has relative maxima at $x = -2$ and at $x = 2$.
- (E) It cannot be determined if f has any relative extrema.

10.

Let $F(x)$ be an antiderivative of $\frac{(\ln x)^3}{x}$. If $F(1) = 0$, then $F(9) =$

- (A) 0.048
- (B) 0.144
- (C) 5.827
- (D) 23.308
- (E) 1,640.250

Free Response

11. 2009—BC6B (No Calculator)

The function f is defined by the power series

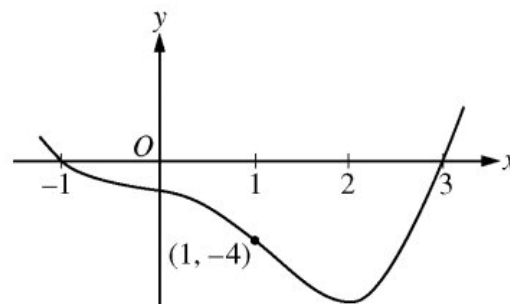
$$f(x) = 1 + (x + 1) + (x + 1)^2 + \cdots + (x + 1)^n + \cdots = \sum_{n=0}^{\infty} (x + 1)^n$$

for all real numbers x for which the series converges.

- Find the interval of convergence of the power series for f . Justify your answer.
- The power series above is the Taylor series for f about $x = -1$. Find the sum of the series for f .
- Let g be the function defined by $g(x) = \int_{-1}^x f(t) dt$. Find the value of $g\left(-\frac{1}{2}\right)$, if it exists, or explain why $g\left(-\frac{1}{2}\right)$ cannot be determined.
- Let h be the function defined by $h(x) = f(x^2 - 1)$. Find the first three nonzero terms and the general term of the Taylor series for h about $x = 0$, and find the value of $h\left(\frac{1}{2}\right)$.

12. 2009—AB/BC5B (No Calculator)

Let f be a twice-differentiable function defined on the interval $-1.2 < x < 3.2$ with $f(1) = 2$. The graph of f' , the derivative of f , is shown above. The graph of f' crosses the x -axis at $x = -1$ and $x = 3$ and has a horizontal tangent at $x = 2$. Let g be the function given by $g(x) = e^{f(x)}$.



Graph of f'

- Write an equation for the line tangent to the graph of g at $x = 1$.
- For $-1.2 < x < 3.2$, find all values of x at which g has a local maximum. Justify your answer.
- The second derivative of g is $g''(x) = e^{f(x)}[(f'(x))^2 + f''(x)]$. Is $g''(-1)$ positive, negative, or zero? Justify your answer.
- Find the average rate of change of g' , the derivative of g , over the interval $[1, 3]$.