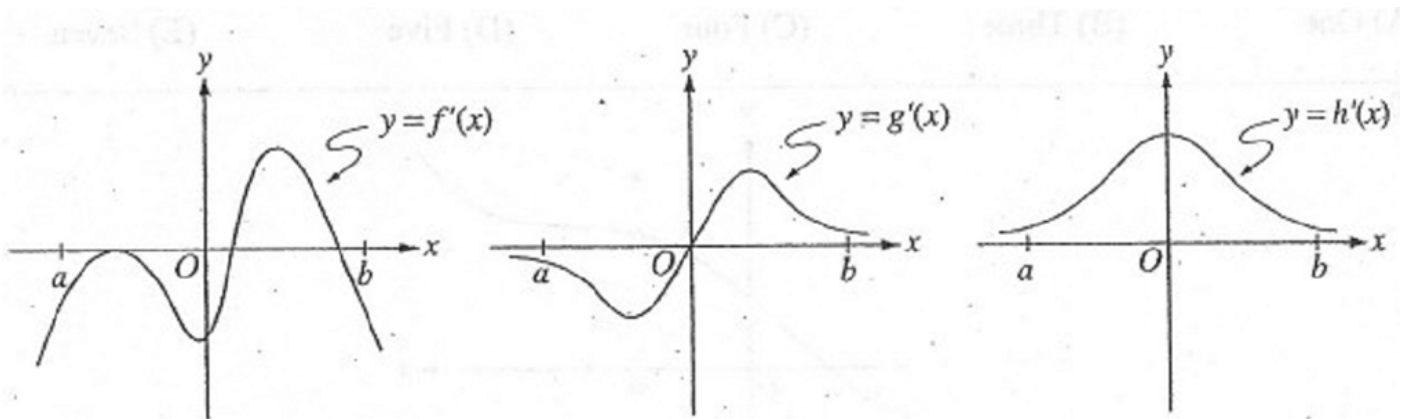


AB Review 07, No Calculator Permitted, unless specified to the contrary.

1. (Calculator Permitted) Let f be the function given by $f(x) = 3e^{2x}$ and let g be the function given by $g(x) = 6x^3$. At what value of x do the graphs of f and g have parallel tangent lines?
(A) -0.701 (B) -0.567 (C) -0.391 (D) -0.302 (E) -0.258
2. The radius of a circle is decreasing at a constant rate of 0.1 centimeters per second. In terms of the circumference C , what is the rate of change of the area of the circle, in square centimeters per second?
(A) $-(0.2)\pi C$ (B) $-(0.1)C$ (C) $-\frac{(0.1)C}{2\pi}$ (D) $(0.1)^2 C$ (E) $(0.1)^2 \pi C$
3. (Calculator Permitted) The first derivative of a function f is given by $f'(x) = \frac{\cos^2 x}{x} - \frac{1}{5}$. How many critical values does f have on the open interval $(0, 10)$?
(A) One (B) Three (C) Four (D) Five (E) Seven
4. $\lim_{x \rightarrow \infty} \frac{(2x-1)(3-x)}{(x-1)(x+3)}$ is
(A) -3 (B) -2 (C) 2 (D) 3 (E) nonexistent

5. Let f be the function given by $f(x) = |x|$. Which of the following statements about f are true?
- I. f is continuous at $x = 0$.
 - II. f is differentiable at $x = 0$.
 - III. f has an absolute minimum at $x = 0$.
- (A) I only (B) II only (C) III only (D) I and III only (E) II and III only

6. If f is a continuous function and if $F'(x) = f(x)$ for all real numbers x , then $\int_1^3 f(2x) dx =$
- (A) $2F(3) - 2F(1)$ (B) $\frac{1}{2}F(3) - \frac{1}{2}F(1)$ (C) $2F(6) - 2F(2)$ (D) $F(6) - F(2)$ (E) $\frac{1}{2}F(6) - \frac{1}{2}F(2)$



7. The graphs of the derivatives of the functions f , g , and h are shown above. Which of the functions f , g , or h have a relative maximum on the open interval $a < x < b$?
- (A) f only (B) g only (C) h only (D) f and g only (E) f , g , and h

8. If $\frac{dy}{dt} = ky$ and k is a nonzero constant, then y could be

- (A) $2e^{kty}$ (B) $2e^{kt}$ (C) $e^{kt} + 3$ (D) $kt y + 5$ (E) $\frac{1}{2}ky^2 + \frac{1}{2}$

9. If $f(x) = (x-1)(x^2+2)^3$, then $f'(x) =$

- (A) $6x(x^2+2)^2$ (B) $6x(x-1)(x^2+2)^2$ (C) $(x^2+2)^2(x^2+3x-1)$
(D) $(x^2+2)^2(7x^2-6x+2)$ (E) $-3(x-1)(x^2+2)^2$

10. A particle moves along the x -axis with velocity given by $v(t) = 3t^2 + 6t$ for time $t \geq 0$. If the particle is at position $x = 2$ at time $t = 0$, what is the position of the particle at $t = 1$?

- (A) 4 (B) 6 (C) 9 (D) 11 (E) 12

11. (2003, AB-6) Let f be the function defined by

$$f(x) = \begin{cases} \sqrt{x+1} & \text{for } 0 \leq x \leq 3 \\ 5-x & \text{for } 3 < x \leq 5 \end{cases}$$

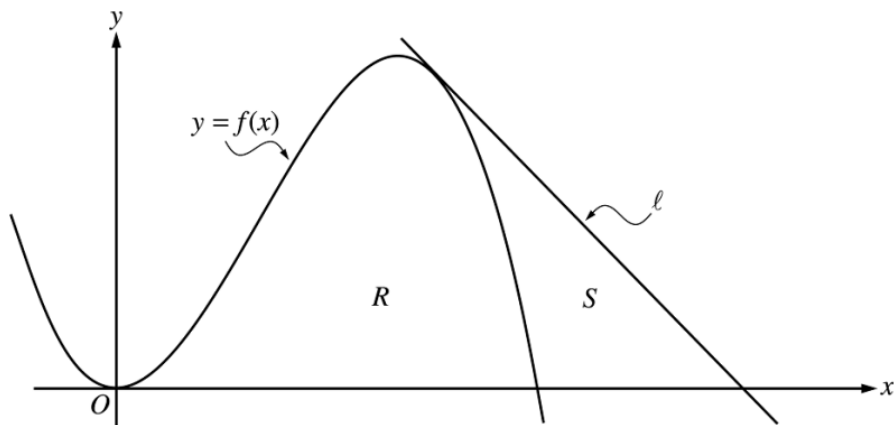
(a) Is f continuous at $x = 3$? Explain why or why not.

(b) Find the average value of $f(x)$ on the closed interval $0 \leq x \leq 5$.

(c) Suppose the function g is defined by

$$g(x) = \begin{cases} k\sqrt{x+1} & \text{for } 0 \leq x \leq 3 \\ mx+2 & \text{for } 3 < x \leq 5 \end{cases}$$

Where k and m are constants. If g is differentiable at $x = 3$, what are the values of k and m ?



12. (2003B, AB/BC-1) (Calculator Permitted) Let f be the function given by $f(x) = 4x^2 - x^3$, and let ℓ be the line $y = 18 - 3x$, where ℓ is tangent to the graph of f . Let R be the region bounded by the graph of f and the x -axis, and let S be the region bounded by the graph of f , the line ℓ , and the x -axis, as shown above.

(a) Show that ℓ is tangent to the graph of $y = f(x)$ at the point $x = 3$.

(b) Find the area of S .

(c) Find the volume of the solid generated when R is revolved about the x -axis.