Déjà Vu, It's Algebra 2!

Lesson 12

Quadratic Functions: Reflections & Dilations, Roots, Max & Mins

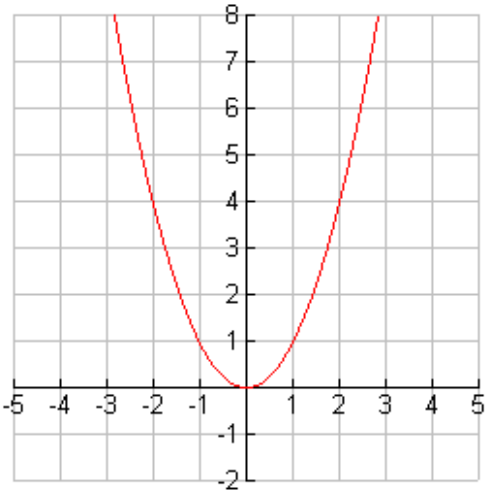
REFLECTIONS

of $f(x) = x^2$

Reflection across *y*-axis

$f(-x) = (-x)^2$

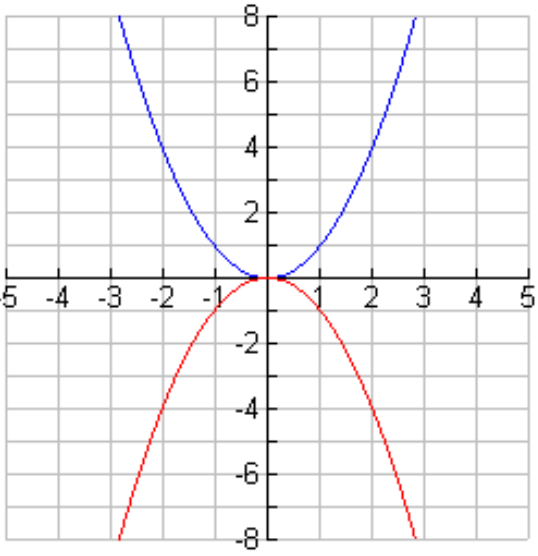
Input values exchange



Reflection across *x*-axis

$-f(x) = -x^2$

Output values exchange



DILATIONS: STRETCHES & COMPRESSIONS

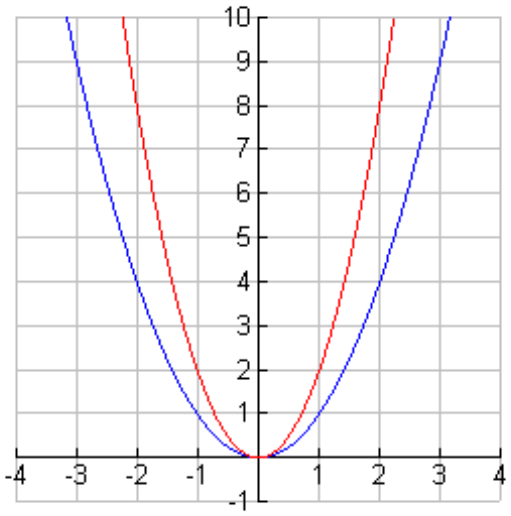
of $f(x) = x^2$

Vertical Dilation for $a > 0$

$f(x) = ax^2$

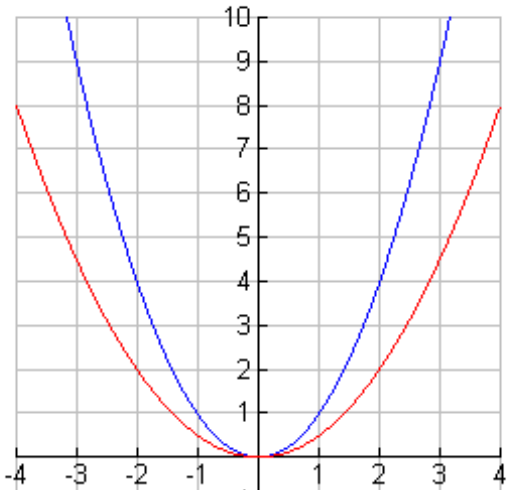
If $a > 1$
Vertical Stretch
away from x-axis

Ex) $g(x) = 2x^2$



If $0 < a < 1$
Vertical Compression
towards x-axis

Ex) $g(x) = \frac{1}{2}x^2$

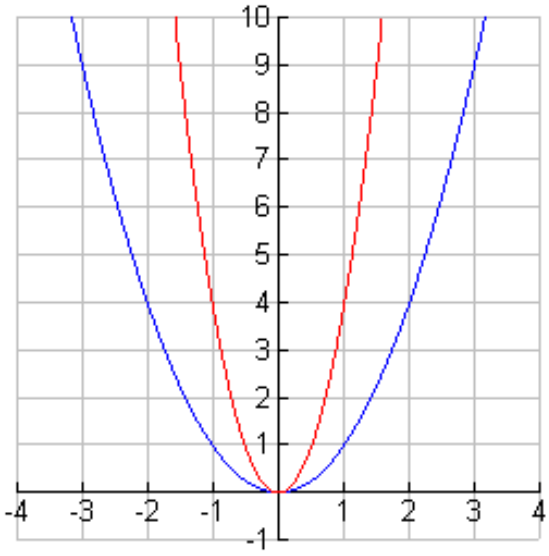


Horizontal Dilation for $b > 0$

$f(bx) = (bx)^2$

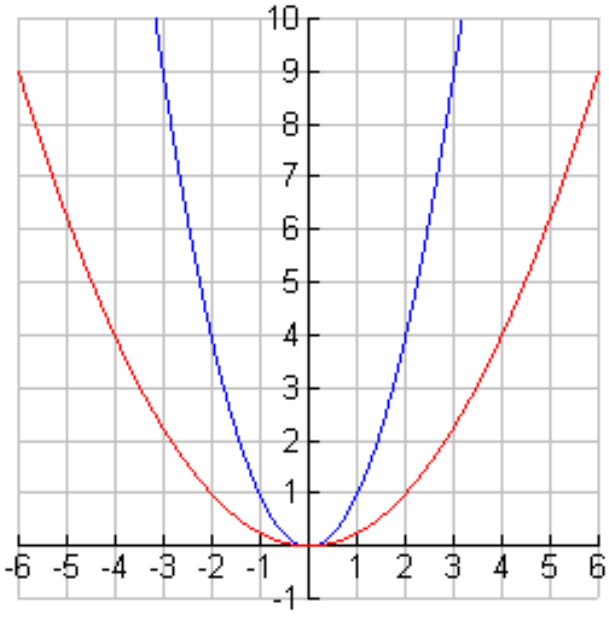
If $b > 1$
Horizontal compression towards y-axis

Ex) $g(x) = (2x)^2$



If $0 < b < 1$
Horizontal stretch away from y-axis

Ex) $g(x) = \left(\frac{1}{2}x\right)^2$



Example:

Sketch the graph of $f(x) = -3x^2$

Mathematical "Synonyms"

- x-intercpets of the graph of a parabola
- roots of a quadratic function, $f(x)$
- zeros of a quadratic, $f(x)$
- solutions to the equation $f(x) = 0$

These values are generally more difficult to find than the y-intercpets, are much more meaningful, in terms of real-world applications.

Factoring is one way to solve quadratic equations:

Example:

Find the zeros of $f(x) = 2x^2 + 2x - 12$

Example:

Find the roots of the following equation.

$g(x) = -3x^2 - 9x$

Example:

Find the x-intercepts of the following equation.

$h(x) = 2x^2 - 8$

Déjà RE-Vu

Application

The height and velocity of a ball thrown straight up with an initial velocity of 28 feet per second from an initial height of 4 feet can be modeled by the following respective equations:

$$h(t) = -16t^2 + 28t + 4$$

$$v(t) = -32t + 28$$

a) What is the maximum height of the ball?
b) At what time does the ball reach its maximum height?
c) How long is the ball in the air?
d) What is the velocity of the ball as it hits the ground?

References:
All images created with TI-Interactive software or TI-83+ calculator

For more information on applications of parabolas, check out the following website:
http://www.pen.k12.va.us/Div/Winchester/jhhs/math/lessons/calc2004/apppara b.html