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word "ratio" in

"rational."





Rational Expressions: Operations & Equations

A rational number is a quotient of two integers Ex) $\frac{4}{6}$, $-\frac{1}{5}$, 1.5, 0.3333..., 7 Notice the key

A rational expression is a quotient of two polynomials

Ex) $\frac{x+3}{x^2+x-2}$, $\frac{4x^5}{6x^7}$, $\frac{4}{3}x$, x^5-x , 8

The following are **NOT** rational expressions. Why not?

Ex)
$$\frac{\sqrt{x}}{3x+1}$$
, $\frac{4x^3+3x^2}{2^x-2x}$, $\frac{\ln x}{x}$

Just as we did with rational numbers, we can simplify rational expressions by dividing out common factors!!!!! (we cannot divide out common terms!)

Review:

A Factor is a number or variable that is multiplied or divided to another number or variable in an expression.

A Term is an expression that is added or subtracted to another expression.

Example:

$$\frac{66}{63} = \frac{60+6}{60+3} = \frac{60+6}{60+3} = \frac{6}{3} = 2$$

Example:

Simplify the following rational expressions.

a)
$$\frac{5}{15} + \frac{x^5}{x^2} + \frac{6x}{4x^3} + \frac{2+x}{7+x}$$
 b) $\frac{x^2 + x - 12}{x^2 + 6x + 8}$

Because we now have ratios of polynomials, we likely have denominators with variables in them. Certain values of the variables MIGHT make the denominator zero. These values will make the expression undefined. WE MUST FIND ANY SUCH VALUES IN THE <u>ORIGINAL</u> EXPRESSION.

Example:

Find the values for which the rational expressions are undefined, then simplify.

a)
$$\frac{2x}{x^2}$$
 b) $\frac{x^2 - 3x - 10}{2x^2 + 5x + 2}$ c) $\frac{x - 2}{2 - x}$

We may also multiply and divide rational expressions in the same fashion we did with rational numbers.

Examples:

Perform the indicated operation and simplify.

a)
$$\frac{3x^5y^3}{2x^3y^7} \cdot \frac{10x^3y^4}{9x^2y^5}$$
 b) $\frac{x-3}{4x+20} \cdot \frac{x+5}{x^2-9}$





We can review our new skills in a new context: Solving rational equations!!!

Examples: Solve

a)
$$\frac{x^2-25}{x-5}=14$$

b)
$$\frac{x^2 + 3x - 10}{x - 2} = 7$$